

1. A second order system with an initial condition of  $\begin{bmatrix} 2 \\ 3 \end{bmatrix}$  without any external input. The state transition

matrix for the system is given by  $\begin{bmatrix} e^{-2t} & 0 \\ 0 & e^{-t} \end{bmatrix}$ . The state of the system at the end of 1 second is given by

- (a)  $\begin{bmatrix} 0.271 \\ 1.100 \end{bmatrix}$     (b)  $\begin{bmatrix} 0.135 \\ 0.368 \end{bmatrix}$     (c)  $\begin{bmatrix} 0.271 \\ 0.736 \end{bmatrix}$     (d)  $\begin{bmatrix} 0.135 \\ 1.100 \end{bmatrix}$

2. The following equation defines a separately excited dc motor in the form of differential equation

$$\frac{d^2\omega}{dt^2} + \frac{B}{J} \frac{d\omega}{dt} + \frac{K^2}{LJ} \omega = \frac{K}{LJ} V_a$$

The above equation may be recognized in the state-space form as follows

$$\begin{bmatrix} \frac{d^2\omega}{dt^2} \\ \frac{d\omega}{dt} \end{bmatrix} = P \begin{bmatrix} \frac{d\omega}{dt} \\ \omega \end{bmatrix} + QV_a$$

Where the P matrix is given by

- (a)  $\begin{bmatrix} -\frac{B}{J} & -\frac{K^2}{LJ} \\ 1 & 0 \end{bmatrix}$     (b)  $\begin{bmatrix} -\frac{K^2}{LJ} & -\frac{B}{J} \\ 0 & 1 \end{bmatrix}$     (c)  $\begin{bmatrix} 0 & 1 \\ -\frac{K^2}{LJ} & -\frac{B}{J} \end{bmatrix}$

- (d)  $\begin{bmatrix} 1 & 0 \\ -\frac{B}{J} & -\frac{K^2}{LJ} \end{bmatrix}$

3. The state variable description of a linear autonomous system is,  $\dot{X}=AX$ , where X is two dimensional state

vector and A is the system matrix given by  $A = \begin{bmatrix} 0 & 2 \\ 2 & 0 \end{bmatrix}$ . The roots of the characteristic equation are

- (a) -2 and +2    (b) -j2 and +j2    (c) -2 and -2    (d) +2 and +2

Statement for linked answer question 4 & 5

The state space equation of a system is described by  $\dot{x} = Ax + Bu, Y = Cx$

Where  $x$  is state vector,  $u$  is output and  $A = \begin{bmatrix} 0 & 1 \\ 0 & -2 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, C = \begin{bmatrix} 1 & 0 \end{bmatrix}$

4. The transfer function  $G(s)$  of this system will be

- (a)  $\frac{s}{s(s+2)}$  (b)  $\frac{s+1}{s(s-2)}$  (c)  $\frac{s}{(s-2)}$  (d)  $\frac{1}{s(s+2)}$

5. A unity feedback is provided to the above system  $G(s)$  to make it closed loop system as shown in the figure.



For a unit step input  $r(t)$ , the steady state error in the input will be

- (a) 0 (b) 1 (c) 2 (d)  $\infty$

6. A linear time invariant system is described by the following dynamic equation

$$\dot{x}(t)/dt = Ax(t) + Bu(t) \quad y(t) = Cx(t)$$

where  $A = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix}, B = \begin{bmatrix} 0 \\ 1 \end{bmatrix}, C = \begin{bmatrix} 1 & 1 \end{bmatrix}$

the system is

- (a) Both controllable and observable (b) Controllable but unobservable (c) Observable but uncontrollable  
(d) Both uncontrollable and uncontrollable

7. Let  $X = \begin{bmatrix} 1 & 2 \\ 0 & 1 \end{bmatrix} x + \begin{bmatrix} 0 \\ 1 \end{bmatrix} U$

$$U = \begin{bmatrix} b, 0 \end{bmatrix}$$

Where b is unknown constant

This system is

- (a) Observable for all values of b (b)unobservable for all values of b (c)observable for all non-zero values of b (d)unobservable for all non-zero values of b

8. the state-space representation in phase-variable form for the transfer function

$$G(s) = \frac{2s+1}{s^2+7s+9}$$

(a)  $\begin{bmatrix} 0 & 1 \\ -9 & -7 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u ; y = \begin{bmatrix} 1 & 2 \end{bmatrix} \mathbf{x}$  (b)  $\begin{bmatrix} 1 & 0 \\ -9 & -7 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u ; y = \begin{bmatrix} 0 & 1 \end{bmatrix} \mathbf{x}$

(c)  $\begin{bmatrix} -9 & 0 \\ 0 & -7 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u ; y = \begin{bmatrix} 2 & 0 \end{bmatrix} \mathbf{x}$  (d)  $\begin{bmatrix} 9 & -7 \\ 1 & 0 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u ; y = \begin{bmatrix} 1 & 2 \end{bmatrix} \mathbf{x}$

9. Consider the single input, single output system with its state variable representation :

$$\begin{bmatrix} -1 & 0 & 0 \\ 0 & -2 & 0 \\ 0 & 0 & -3 \end{bmatrix} \mathbf{x} + \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} U$$

$$Y = \begin{bmatrix} 1 & 0 & 2 \end{bmatrix} \mathbf{x}$$

The system is

- (a) Neither controllable nor observable (b)Controllable but not observable (c)Uncontrollable but observable (d)Both controllable and observable

10. A particular control system is described by the following state equations :

$$\dot{X} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} X + \begin{bmatrix} 0 \\ 1 \end{bmatrix} U \quad \text{and } Y = \begin{bmatrix} 2 & 0 \end{bmatrix} X$$

The transfer function of this system is :

(a)  $\frac{Y(s)}{U(s)} = \frac{1}{2s^2 + 3s + 1}$

(b)  $\frac{Y(s)}{U(s)} = \frac{2}{2s^2 + 3s + 1}$

(c)  $\frac{Y(s)}{U(s)} = \frac{1}{s^2 + 3s + 2}$

(d)  $\frac{Y(s)}{U(s)} = \frac{4}{2s^2 + 3s + 2}$